



Modelling the food sector

We postulate an increasing and concave production function for the food sector: $f'_F > 0$ and $f''_F < 0$
The program of the representative firm of the food sector can be written as:

$$\max_{x_F} p_F f_F(x_F) - w(X)x_F$$

Modelling the biofuel sector

$$f_E(x_E) = \gamma_E x_E,$$

where γ_E is a positive parameter.

Assume that the energy firm cannot operate without subsidy since:

$$p_E \gamma_E < w(X_0),$$

where X_0 is the total quantity of crops bought by the food firm when no biofuel is produced.

⇒ The energy sector receives a subsidy:

$$\sigma = w(X) - p_E \gamma_E$$

in order to attain the level Q/γ_E .

Quantity of food crops vs energy crops

As x_E increases, the aggregate quantity X increases and x_F decreases, i.e.

$$\frac{dx_F}{dx_E} \in [-1, 0]$$

Hence:

$$\frac{dX}{dx_E} = 1 + \frac{dx_F}{dx_E} > 0$$

Who gains, who loses?

As x_E increases

- The agricultural surplus increases
- The consumers' surplus decreases
- The agro-food industry may gain ($|\epsilon_F| < 1$) or lose ($|\epsilon_F| > 1$)
- The biofuel sector makes no profit (perfectly adjusted subsidy)

The social welfare function

The regulator maximizes the following SWF:

$$\max_{x_E} \bar{\Pi}_A + \Pi_C(x_E) + \Pi_F(x_E) - (1+\lambda)\{T(x_E) + [\bar{\Pi}_A - \Pi_A(x_E)]\} + qx_E$$

s.t. $x_E \geq Q/\gamma_E$

The optimal production of energy crops

The first-order condition of the SWF leads to the following equation:

$$\lambda x_F w'(X) \frac{dX}{dx_E} + q - (1+\lambda)\{w(X) - p_E \gamma_E\} \leq 0 (x_E^* \geq 0)$$

This equation determines the optimal quantity of energy crops x_E^* .

Comparison with the Pigovian level

If $\lambda = 0$, we would have the following first-order condition:

$$q - [w(X) - p_E \gamma_E] \leq 0 (x_E^* \geq 0)$$

which is the Pigovian rule: the optimal subsidy should equalize the marginal benefit of GHG mitigation.

The real cost of the biofuel program

Hence, if $\lambda > \lambda_N$, x_E^* is strictly positive and we have:

- if $Q/\gamma_E < x_E^*$, the biofuel constraint is slack and it is optimal to produce energy crops up to x_E^* .
- If $Q/\gamma_E > x_E^*$, the biofuel constraint is binding. However, the real cost of the environmental program should be calculated only on the residual quantity $Q/\gamma_E - x_E^*$.

The social welfare function with imports

The program has now the following form:

$$\max_{x_E, x_I} \bar{\Pi}_A - (1+\lambda)\{T(x_E+x_I) + (\bar{\Pi}_A - \Pi_A(x_E))\} + \Pi_F(x_E) + q(x_E+x_I)$$

$$s.t. x_E + x_I \geq Q/\gamma_E$$

Imports

First-order conditions of the program:

$$\lambda x_F w'(X) \frac{dX}{dx_E} - (1+\lambda)\{w(X) - p_E \gamma_E\} + q \leq 0 (x_E^* \geq 0),$$

$$-(1+\lambda)(\bar{w} - p_E \gamma_E) + q \leq 0 (x_I^* \geq 0)$$

Imports

if $\lambda > \lambda_N$, x_E^* is strictly positive and we have:

- if $Q/\gamma_E < x_E^*$, the biofuel constraint is slack and it is optimal to produce energy crops up to x_E^* .
- If $Q/\gamma_E > x_E^*$, the biofuel constraint is binding and it is optimal to produce energy crops domestically at level $\hat{x}_E > x_E^*$. Importations of raw material are given by $x_I^* = Q/\gamma_E - \hat{x}_E$.
- The internal price of agricultural feedstock verifies $w(X) > \bar{w}$ leading to subsidies $\sigma_E > \sigma_I$

Biofuels and the environment

Environmental policies and biofuel production

- Positive externalities of biofuels concerning GHG emissions.
- But: negative externalities in agricultural production (fertiliser and phytosanitary products), due to a more important feedstock production.

Let $C(X,e)$ denote the cost function of the representative farmer ($C_X = w$.)

Biofuels and the environment

The regulator chooses the optimal quantity of energy crops and the optimal level of environmental standard \bar{e} . Neglecting the constraint on the biofuel production, the agency program can thus be written as:

$$\max_{x_E, x_F, \bar{e}} \bar{\Pi}_A + CS + \Pi_F - (1+\lambda)[(C_X - p_E \gamma_E)x_E + \bar{\Pi}_A - \Pi_A] + B(x_E) - D(\bar{e})$$

s.t. EQFood

Biofuels and the environment

If $\lambda > \lambda_s$, and $Q = 0$, the optimal policy \bar{e}^* , x_E^* and x_F^* is implicitly defined by

$$(1+\lambda)[C_X - p_E \gamma_E] - q = \lambda x_F C_{XX} dX/dx_E = -\frac{C_{XX}}{C_{Xe}} \{-(1+\lambda)C_e - D'(\bar{e})\}$$

⇒ The optimal standard \bar{e}^* is more stringent than the Pigovian level.

Conclusion

Biofuel policies might deeply alter agricultural and environmental policies.

- The support to the agricultural sector could be lowered (as the subsidies for biofuels partly substitute for them).
- Environmental issue will be crucial, with an intensive production of energy crops.